

## Learning Objectives

1. Understand and apply logic for crashing projects
2. Schedule projects using probabilistic task time estimates

## Advanced Project Scheduling Techiniques

- Crashing: adding resources to efficiently speed up a project
- Probabilistic Scheduling: using statistics to model uncertainty in estimating various project outcomes



## Project Crashing

Step in crashing a project:
1.List the crash costs for each task in the project.
2.Choose the task or combination of tasks on the critical. path that has the lowest crash cost, and reduce that task's duration by one period.
3.Update the lengths of all affected paths in the network. Identify any paths that have become critical.
4.Repeat the process until the plan meets the required deadline or until the cost of reducing the project length exceeds the benefit.

## Project Crashing

TABLE 16S-1 Crash Schedule for Planning System Installation Project

| Task | Current Planned <br> Duration | Minimum <br> Duration | Crash Cost <br> per Day |
| :--- | :---: | :---: | :---: |
| *Select System Modules | 9 | 6 | $\$ 1200$ |
| Prepare Data | 5 | 4 | $\$ 200$ |
| *Set System Protocols | 3 | 1 | $\$ 500$ |
| *Populate System Data | 5 | 3 | $\$ 700$ |
| Prepare Documentation | 14 | 10 | $\$ 400$ |
| Design Training Program | 2 | 2 | - |
| Hold Training Sessions | 1 | 1 | - |
| *Test System | 6 | 3 | $\$ 600$ |
| *Debug System | 4 | 2 | $\$ 800$ |
| *Pilot Test | 3 | 2 | $\$ 900$ |
| *Hold "Go Live" Meeting | 1 | 1 | - |

*Task is on the critical path

## Project Crashing

TABLE 16S-2 Summary of Crash Plan for the Planning System Installation Project

|  | Activity to Crash | Crash Cost | Critical Path Length | Notes: |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  |  | 31 days | No tasks crashed |
| 1 | Set System Protocols | \$ 500 | 30 days | Cheapest task on critical path |
| 2 | Set System Protocols | \$ 500 | 29 days | Cannot crash this task any further |
| 3 | Test System | \$ 600 | 28 days | Cheapest task on critical path |
| 4 | Test System | \$ 600 | 27 days | Prepare Documentation becomes on a critical path |
| 5 | Pilot Test | \$ 900 | 26 days | Crashing this task reduces both critical paths. Planned deadline met. |
|  | Total Cost: | \$3100 |  |  |



## Probabilistic Estimates

- Best Case: estimate of task time if all goes as planned
- Most Likely: most probable task time
- Worst Case: estimate of task time if all possible delays are realized


## Probabilistic Estimates

TABLE 16S-3 Probabilistic Time Estimates for the Planning System Installation Project

| Task | Best Case <br> Duration | Most Likely <br> Duration | Worst Case <br> Duration |
| :--- | :---: | :---: | :---: |
| *Select System Modules | 7 | 9 | 15 |
| Prepare Data | 4 | 5 | 10 |
| *Set System Protocols | 2 | 3 | 5 |
| *Populate System Data | 3 | 5 | 7 |
| Prepare Documentation | 10 | 14 | 16 |
| Design Training Program | 2 | 2 | 3 |
| Hold Training Sessions | 1 | 1 | 2 |
| "Test System | 4 | 6 | 8 |
| *Debug System | 2 | 4 | 6 |
| *Pilot Test | 2 | 3 | 4 |
| *Hold "Go Live" Meeting | 1 | 1 | 1 |

*Task is on the critical path

## Probabilistic Estimates

$$
\begin{aligned}
& t_{i}=\frac{\text { worst }+\left(4^{*} \text { most likly }\right)+\text { best }}{6} \\
& \sigma_{i}=\frac{(\text { worst }- \text { best })}{6} \\
& t_{\text {path }}=\Sigma t_{i} \\
& \sigma_{\text {path }}=\sqrt{\Sigma_{\sigma_{i}^{2}}^{2}} \\
& z=\left(\text { t arget completion time }-t_{\text {path }}\right) / \sigma_{\text {path }}
\end{aligned}
$$

## Probabilistic Estimates

TABLE 16S-4
Expected Duration and
Standard Deviations for
Planning System Instal-
lation Project

| Task | Best Case Duration | Most Likely Duration | Worst Case Duration | Expected Duration | Standard Deviation |
| :---: | :---: | :---: | :---: | :---: | :---: |
| *Select System Modules | 7 | 9 | 15 | 9.67 | 1.33 |
| Prepare Data | 4 | 5 | 10 | 5.67 | 1 |
| *Set System Protocols | 2 | 3 | 5 | 3.17 | 0.5 |
| *Populate System Data | 3 | 5 | 7 | 5 | 0.67 |
| Prepare Documentation | 10 | 14 | 16 | 13.67 | 1 |
| Design Training Program | 2 | 2 | 3 | 2.17 | 0.17 |
| Hold Training Sessions | 1 | 1 | 2 | 1.17 | 0.17 |
| *Test System | 4 | 6 | 8 | 6 | 0.67 |
| *Debug System | 2 | 4 | 6 | 4 | 0.67 |
| * Pilot Test | 2 | 3 | 4 | 3 | 0.33 |
| *Hold "Go Live" Meeting | 1 | 1 | 1 | 1 | 0 |

## Probabilistic Estimates

The most likely time for completion is day 31, and it must be done day 33. Given the previous data, what is the probability we will be on time?
$t_{i}=(15+4 * 9+7) / 6=9.67$ days
$\sigma_{\mathrm{i}}=(15-7) / 6=1.33$ days
$\mathrm{t}_{\text {path }}=9.67+3.17+5+6+4+3+1=31.84$ days
$\sigma_{\text {path }}=1.86$ days
$\mathrm{z}=(33-31.84) / 1.86=.624$ or $73 \%$ (from z table)

## Advanced Project Management Summary

1. There are time-cost trade-offs.
2. The probability of finishing a task or a project on time can be calculated.
