



Learning Objectives

1. Apply quality management tools for problem solving
2. Identify the importance of data in quality management

Quality Improvement tools

- **Variable Data** (continuous): quantifiable conditions along a scale, such as speed, length, density, etc.
- **Attribute Data** (discrete): qualitative characteristic or condition, such as pass/fail, good/bad, go/no go.

6S-3

Quality Improvement tools

| Quality Tools | Typical Usage |
|-----------------------------|---|
| Histogram | Uncover patterns in data variability |
| Cause and effect analysis | Uncover contributors to problem; facilitate brainstorming |
| Check sheets | Identify frequency and location of problems |
| Pareto analysis | Identify most critical cause of problems |
| Scatter diagrams | Determine relationship between variables |
| Process flow analysis | Graph of process steps |
| Process capability analysis | Compare process variability and specifications |
| Process control charts | Monitor process output for 'normality' of variance |
| Taguchi method/DoE | Track effects of different factors on outputs |

Table 6S-1

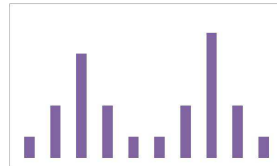
6S-4

Histograms

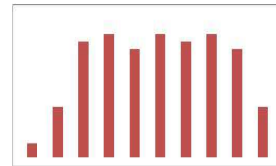
Review center, width and shape



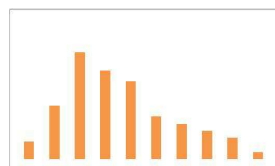
Bell-shaped
Normal distribution



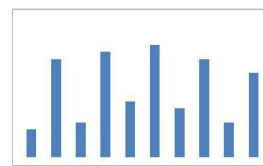
Double peak
Two processes?



Plateau
Combined data sets?



Skewed
System limitation?



Comb
Error in process or
data collection

Figure 6S-1

6S-5

Cause and Effect Diagram

1. Identify the problem to examine
2. Identify the major categories of causes
3. Identify more specific causes
4. Circle likely causes
5. Verify the causes

Figure 6-1

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Pareto Analysis

- Separates the critical few from the trivial many
 1. Identify categories about which to collect data
 2. Gather data and calculate frequency of observations in each category for an appropriate time period
 3. Sort into descending order by percentage
 4. Graph and identify the few areas that account for most of the variation

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Pareto Analysis

FIGURE 6S-4
Pareto Analysis for
Pear Computers

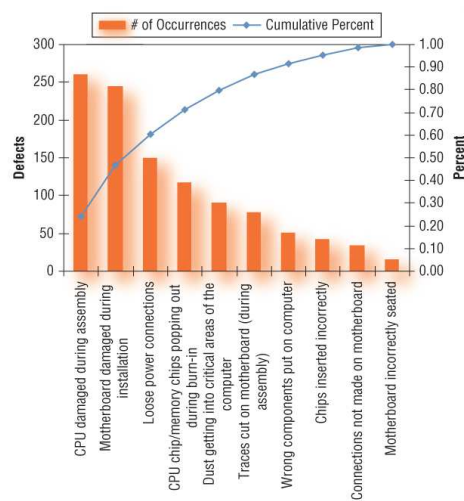


Figure 6S-4

6S-10

Scatter Diagram

- Graphical representation of the relationship between two variables

FIGURE 6S-5
Scatter Diagram for
Conveyor Speed and
Cut Length

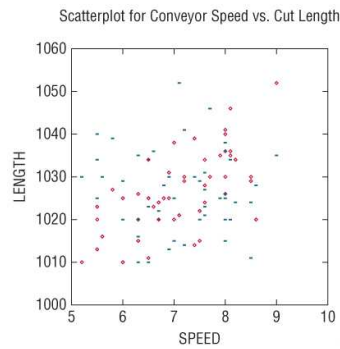


Figure 6S-5

6S-11

Process Flow Diagram

FIGURE 3S-3 Process Flow Diagram: Dry-Mill Ethanol Process for Converting Corn to Fuel Grade Ethanol[®]

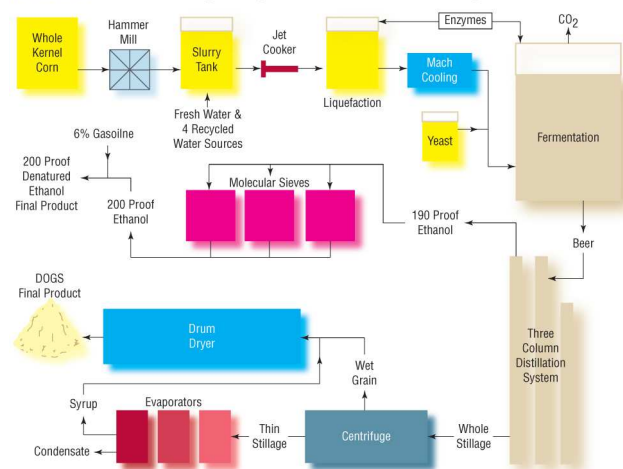


Figure 3S-3

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Process Capability (C_p)

- Assess ability of a process to meet (or exceed) design specifications

$$C_p = \frac{\text{Specification width}}{\text{Process width}} = \frac{S}{P}$$

Where:

S = Upper specification limit – Lower specification limit

P = 6σ (99.7% of variation)

σ = Standard deviation of process output

Figure 6S-5 6S-13

Process Capability (C_p)

$C_p < 1$ observed spread larger than desired spread

$C_p = 1$ observed and desired spread exactly equal

$C_p > 1$ desired spread larger than observed spread

When $\pm 3\sigma$ is used to calculate C_p

$C_p = 1.00$ is 3σ quality (3σ to either side)

$C_p = 1.33$ is 4σ quality

$C_p = 1.67$ is 5σ quality

$C_p = 2.00$ is 6σ quality

Figure 6-1 6S-14

Process Capability (C_p)

$$C_p = \frac{20}{6 * 5} = 0.67$$

When $\sigma = 5$ mils,
the process is NOT capable

$$C_p < 1$$

$$C_p = \frac{20}{6 * 2} = 1.67$$

When $\sigma = 2$ mils,
the process IS capable

$$C_p > 1$$

Where:

S = designed to be 1,030 mil +/- 10 mil, so = 20 mils

USL = 1,040 and LSL = 1,020

P = 6σ (99.7% of variation)

Figure 6S-5 6S-15

Process Capability (C_p)

FIGURE 6S-6
Sample Distributions
and their Associated
 C_p Measures

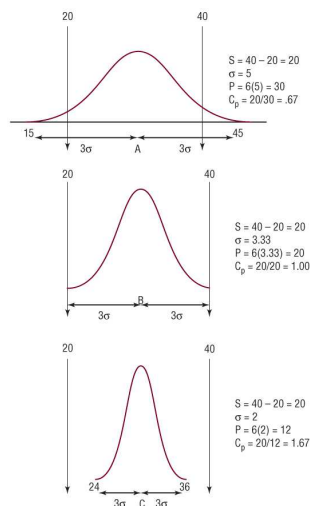


Figure 6S-6 6S-16

Improving on the C_p Statistic with C_{pk}

- C_{pk} : compares process output and specification widths, and examines process centering

$$C_p = \frac{S}{P} = \frac{(USL - LSL)}{6\sigma}$$

$$K = \frac{|D - \bar{X}|}{S/2}$$

$$C_{pk} = (1 - K) * C_p$$

Where:

USL & LSL = Upper & Lower specification limit

D = Center of product specification range = $(USL + LSL)/2$

\bar{X} = Mean of process output distribution

K = Adjustment of centeredness of process and specifications

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Improving on the C_p Statistic with C_{pk}

$$K = \frac{|1030 - 1020|}{20/2} = 1$$

$$C_{pk} = (1 - 1) * 1.67 = 0$$

Process is NOT centered

Where:

USL & LSL = 1,040 and 1,020

S = 20

D = 1,030

\bar{X} = 1,020 (given)

Cp = 1.67 (from previous example)

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Process Capability (C_{pk})

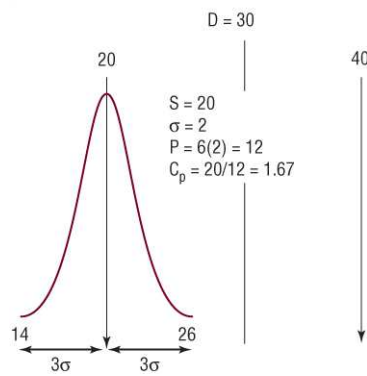


FIGURE 6S-7
Deceptive C_p Value:
The Problem of Lack
of Centering

Figure 6S-7 6S-19

Process Control Charts

- Statistical tool to monitor process output to detect significant changes

FIGURE 6S-8
Process Control Limits

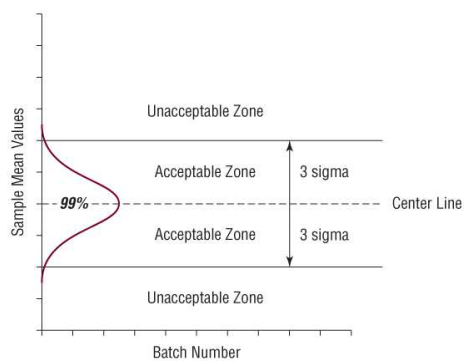


Figure 6S-8 6S-20

Process Control Charts

TABLE 6S-3 Types of Control Charts and Data Covered¹

| Type of Data | Control Chart Used | Types of Data |
|---|---|---|
| Variables— Continuous/ Indiscrete | $\bar{x}-R$ | measurement (inches, mm) volume product weight power consumed |
| Attributes—Discrete | pn (probability of defect)* (number in batch) | number of defects |
| Attributes | P | fraction defective |
| Attributes | U | number of pin holes in pieces of plated sheet, differing in area (area/volume is not fixed) |
| Attributes | C | number of pin holes in a specified area (area is fixed) |

¹Kaoru Ishikawa, *Guide to Quality Control*, Second Revised Edition. (Tokyo: Asian Production Organization, 1982.) Reprinted with permission.

Table 6S-3

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Process Control Charts

- Constructing and using x-bar and R charts

1. Collect data to calculate control limits

2. For each sample, calculate the sample mean $\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$

3. For each sample find the range (R)

4. Calculate the overall 'grand' mean ($\bar{\bar{X}}$)

5. Calculate the mean range (\bar{R})

6. Compare control limits and construct the charts

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Process Control Charts

Equations for the \bar{x} and R charts

\bar{x} chart: *Central line* = $\bar{\bar{x}}$

Lower control limit = $\bar{\bar{x}} - A_2 \bar{R}$

Upper control limit = $\bar{\bar{x}} + A_2 \bar{R}$

R chart: *Central line* = \bar{R}

Lower control limit = $D_3 \bar{R}$

Upper control limit = $D_4 \bar{R}$

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Process Control Charts

- A process has 20 sample means, with a 'grand' mean of 12.14 and an average range of 0.69

TABLE 6S-6 Control Limits Calculated for the Example Control Chart

| Data Points | \bar{x} Chart | R Chart |
|---------------------------|------------------------------------|----------------------------|
| Central Line | 12.14 ms | 0.69 |
| Lower Control Limit (LCL) | $12.14 - 0.577 \cdot 0.69 = 11.74$ | 0 |
| Upper Control Limit (UCL) | $12.14 + 0.577 \cdot 0.69 = 12.54$ | $2.115 \cdot 0.69 = 1.459$ |

Table 6S-6

6S-24

Process Control Charts

FIGURE 6S-9 \bar{X} and R
Chart for the Example
Data Set

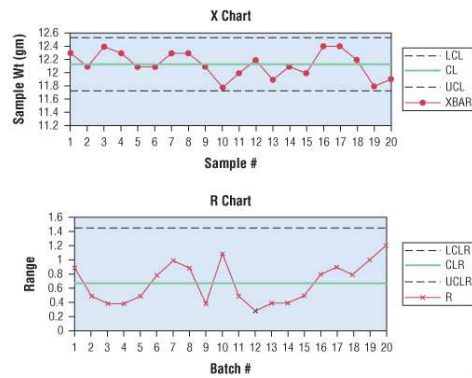


Figure 6S-9

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Taguchi Methods

- Statistical methods for improving the design of a product and the processes that improve it
- Goal is to identify easily controllable factors that can be used to reduce variation

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Managing Quality Summary

1. Effective quality management is data driven
2. There are multiple tools to identify and prioritize process problems
3. There are multiple tools to identify the relationships between variables
4. Process capability compares actual process output with design specifications

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